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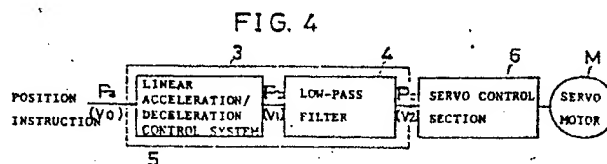
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**(54) METHOD OF CONTROLLING ACCELERATION AND DECELERATION.**

(57) A method of generating a speed command signal which is delivered to a servo motor control unit in a position control apparatus. A given position command signal is applied to a low-pass filter (4) either directly or through a linear acceleration/deceleration unit (3). An output of the low-pass filter (4) is employed as a speed command signal delivered to a control unit (6) for a servo motor (M).



EP 0 139 010 A1

S P E C I F I C A T I O N  
ACCELERATION/DECELERATION CONTROL SYSTEM  
Technical Field

The present invention relates to an  
5 acceleration/deceleration control system of a servo  
motor used in an NC machine tool and a robot.

Background Art

Fig. 1 is a block diagram of a servo motor  
acceleration/deceleration control system. A typical  
10 example of the conventional acceleration/deceleration  
system of this type is an exponential accelera-  
tion/deceleration control system.

In this system, an exponential function type  
acceleration/deceleration control unit is used as an  
15 acceleration/deceleration control section 1 shown in  
Fig. 1. When a position instruction is supplied as a  
displacement  $V_0$  per unit time to the accelera-  
tion/deceleration section 1, i.e., when a pulsed input  
shown in Fig. 2(a) is entered as a value  $V_0$  which is  
20 substantially the same as the velocity, an exponential  
output shown in Fig. 2(b) is obtained.

As shown in this response waveform, an  
acceleration speed is high at a leading edge (indicated  
by  $\alpha$  in Fig. 2) due to the influence of a  
25 high-frequency component, so that a servo control  
section 2 and a load system are subjected to shock,  
resulting in vibrations. As shown in Fig. 2(b), a long  
period of time is required to decelerate and stop the  
servo motor, resulting in inconvenience. For these  
30 reasons, for example, when X- and Y-axis servo motors  
are used to shift a table of a machine tool in an  
arcuated manner, the table has a locus smaller than  
that designated by an instruction.

A linear acceleration/deceleration control system  
35 can be used in place of the exponential accelera-  
tion/deceleration control system. An output waveform  
shown in Fig. 5(b) is obtained in response to a step

input shown in Fig. 5(a). As indicated by this output waveform, an acceleration speed abruptly changes, and a servo control system and a load system are subjected to shock, resulting in vibrations. For example, an arm of a robot or the like continues to vibrate when it is stopped quickly, resulting in inconvenience.

Furthermore, since the servo control system and the load system have natural frequencies, when the servo control system and the load system are driven by frequency components similar to the natural frequencies, respectively, the servo control system and the load system vibrate by themselves. For this reason, vibration of the natural frequency components included in position instruction for the servo control system and the load system must be cut off.

#### Disclosure of Invention

A transfer function in an exponential acceleration/deceleration control section for generating the output shown in Fig. 2(b) in response to the step input shown in Fig. 2(a) is a transfer function  $H(S)$  having a time-lag of first order as follows:

$$H(S) = K/(S + K) \quad \dots(1)$$

where  $K$  is a constant.

This transfer function is obtained by a first-order low-pass filter. The conventional acceleration/deceleration control section 1 given by this transfer function indicates that a low-frequency component included in the position instruction (input) passes through but a high-frequency component is cut off, and that the resultant frequency component as the position instruction is supplied to the servo control section 2. However, as indicated by the output waveform shown in Fig. 2(b), the influence of a high-frequency component occurs at the leading edge or the like to cause an abrupt change in velocity. For this reason, in order to cut off the high-frequency component, a time constant of the transfer function

given by equation (1) must be increased. However, when the time constant is increased, a response time becomes slow, and a time for stopping the servo motor becomes prolonged.

5        This can be overcome by using a higher-order low-pass filter in place of the first-order low-pass filter. In this case, the position instruction to the servo motor is filtered through this higher-order low-pass filter, and the servo motor is driven by the  
10    filtered component. As the low pass filter has a higher order, the natural frequencies of the servo control system and the load system can be cut off, and the high-frequency component is also cut off. As a result, a smooth response waveform and a fast response  
15    can be obtained.

      It is, therefore, a first object of the present invention to provide an acceleration/deceleration control system of a servo motor, wherein a change in velocity can be decreased by using a higher-order  
20    low-pass filter, and a short response time can be obtained with a small delay.

      It is a second object of the present invention to provide an acceleration/deceleration system of a servo motor wherein no vibrations occur and the servo motor  
25    can be operated with a small change in velocity.

      In order to achieve the above objects of the present invention, there is provided an acceleration/deceleration system for controlling acceleration/deceleration of a servo motor by filtering a  
30    position instruction to the servo motor through a low-pass filter of second or higher order.

      According to the acceleration/deceleration control system for controlling linear acceleration/deceleration, the position instruction supplied to the servo  
35    motor is subjected to linear acceleration/deceleration control. The linearly controlled instruction is

filtered through a low-pass filter of second or higher order.

As described above, since the position instruction is supplied to the servo motor through the low-pass  
5 filter of second or higher order, the high-frequency component is cut off, and the natural frequency components of the servo control system and the load system are also cut off. As a result, the servo control system and the load system will neither be  
10 subjected to shock nor generate vibrations. In addition, the servo control system and the load system will not vibrate by themselves. Since a high-order low-pass filter is used, a fast response time can be obtained. For example, unlike the conventional  
15 example, a table or the like of a machine tool will not trace a locus smaller than that specified by the instruction even if it is driven in an arcuated locus.

Brief Description of Drawings

Fig. 1 is a block diagram of an acceleration/de-  
20 celeration control system of a servo motor, Fig. 2 shows waveforms of an input and an output with respect to a conventional exponential acceleration/deceleration control system, Fig. 3 shows input/output waveforms with respect to the acceleration/deceleration control  
25 section when a higher-order low-pass filter is used in this section, Fig. 4 is a block diagram of an embodiment of the present invention when a higher-order low-pass filter is used, Fig. 5 shows input/output waveforms of the respective blocks of the embodiment  
30 shown in Fig. 4, Fig. 6 is a block diagram of a linear acceleration/deceleration control system, Fig. 7 shows input/output waveforms with respect to the system shown in Fig. 6, Fig. 8 is a block diagram of a first-order digital filter, Fig. 9 is a block diagram of a  
35 second-order digital filter, Fig. 10 is a block diagram of a third-order digital filter, and Fig. 11 is a flow chart for explaining an operation of the present

invention when the third-order digital filter is coupled to the linear acceleration/deceleration control section.

#### Best Mode of Carrying Out the Invention

5 The present invention will be described in detail hereinafter.

Transfer functions  $H(S)$  of a higher-order low pass filter can be obtained by a second-order transfer function, a third-order transfer function as a  
10 combination of first- and second-order transfer functions, and a fourth-order transfer function as a combination of second-order transfer functions in the following manner:

$$15 \quad \text{2nd-order } H(S) = \frac{(A_1 W_0)^2}{\{S^2 + (A_1 W_0 / Q_1)S + (A_1 W_0)^2\}} \dots (2)$$

$$\text{3rd-order } H(S) = \{(B_1 W_0) / (S + B_1 W_0)\} \times [(A_1 W_0)^2 / \{S^2 + (A_1 W_0 / Q_1)S + (A_1 W_0)^2\}] \dots (3)$$

$$20 \quad \text{4th-order } H(S) = [(A_1 W_0)^2 / \{S^2 + (A_1 W_0 / Q_1)S + (A_1 W_0)^2\}] \times [(A_2 W_0)^2 / \{S^2 + (A_2 W_0 / Q_2)S + (A_2 W_0)^2\}] \dots (4)$$

where  $A_1$ ,  $A_2$ ,  $B_1$ ,  $Q_1$  and  $Q_2$  are coefficients and  $W_0$  is the angular velocity at a cutoff frequency of the filter.

25 By properly selecting the coefficients (i.e.,  $A_1$ ,  $B_1$  and  $Q_1$ ) of the transfer functions  $H(S)$ , a low-pass filter having a high speed and smooth response and free from vibrations can be obtained. This low-pass filter may be any one of Bessel, Butterworth and Chebyshev  
30 filters.

An optimal low-pass filter for achieving the above objects of the present invention can be obtained such that the coefficients of the Bessel filter are properly selected, and a cutoff frequency of the filter is  
35 selected to cut off the natural frequencies of the servo control system and the load system. This Bessel

low-pass filter is used as the acceleration/deceleration control section 1 in Fig. 1. An output shown in Fig. 3(b) is generated from the acceleration/deceleration section 1 in response to the input waveform of the position instruction, as shown in Fig. 3(a). In this manner, the high-frequency component is cut off from the position instruction, so that a change in output  $V_1$  is smooth. A high acceleration speed at the leading edge of the output will not be obtained. As a result, the time required for decelerating and stopping the servo motor can be shortened.

As a second embodiment of the present invention, a high-order low-pass filter 4 is connected to an output of a linear acceleration/deceleration section 3, as shown in Fig. 4. An output from the low-pass filter 4 drives a servo control section 6 and a servo motor M. This output  $V_2$  becomes smooth, as shown in Fig. 5(c). More particularly, when a pulsed input  $V_0$  shown in Fig. 5(a) is supplied to the linear acceleration/deceleration section 3, the linear acceleration/deceleration section 3 generates an output  $V_1$ , as shown in Fig. 5(a). In the conventional control system, the output  $V_1$  is supplied to the servo control section 6. However, according to the present invention, the output  $V_1$  is supplied to the high-order low-pass filter 4 which then generates the output  $V_2$  whose waveform is illustrated in Fig. 5(c). The output  $V_2$  is then supplied to the servo control section 6. As a result, since the output  $V_2$  whose waveform shown in Fig. 5(c) is smoother than that of the output  $V_1$  shown in Fig. 5(b) is supplied to the servo control section 6, the servo control section 6 and the servo motor M will not receive shock caused by an abrupt change in velocity and will not generate vibrations. In addition, the servo control section 6 and the servo motor M have a fast response time.

As described above, the low-pass filter is used in the acceleration/deceleration control section according to the present invention. In the linear acceleration/deceleration system, the linear acceleration/deceleration section 3 and the low-pass filter 4 constitute an acceleration/deceleration control section 5. As a result, an acceleration/deceleration control system having a fast response time and being free of vibrations can be obtained.

10 An embodiment of the present invention which has the acceleration/deceleration control section 5 consisting of the linear acceleration/deceleration section 3 and the low-pass filter 4 will be described with reference to the accompanying drawings.

15 Digital processing of the linear acceleration/deceleration section 3 will be described with reference to Fig. 6. A position instruction  $P_a$  for each axis is supplied from an interpolation distribution control section or the like to the linear acceleration/deceleration section 3 for each sampling (a sampling period  $T$ ). The linear acceleration/acceleration section 3 has  $(n - 1)$  delay units  $z^{-1}$  (delay of the sampling period  $T$ ) (where  $n$  is a value obtained by dividing by the sampling period  $T$  an acceleration/deceleration time from the beginning to the end of acceleration or deceleration, i.e.,  $n = \tau/T$ ). The position instruction  $P_a$  is added by an adding means 10 to the output from each of the delay units  $z^{-1}$ . A multiplying means 11 multiplies  $1/n$  with a sum from the adding means 10, thus obtaining  $P_b$  as follows:

$$P_b = (P_a + X_1 + X_2 + \dots + X_{n-1})/n \quad \dots(5)$$

For example, if the position instruction  $P_a$ , the sampling period  $T$  and the acceleration/deceleration time are given as 100, 8 msec and 40 msec, respectively,  $n = 40/8 = 5$ . The linear acceleration/deceleration section 3 comprises four delay units  $z^{-1}$ , and the relationship between the input and the



output is shown in Figs. 7(a) and 7(b). In the first sampling cycle,

$P_a = 100$ , and  $X_1$  to  $X_4 = 0$ ,  
therefore,

$$\begin{aligned} P_b &= (P_a + X_1 + X_2 + X_3 + X_4)/n \\ &= 100/5 = 20 \end{aligned}$$

In the second sampling cycle,

$P_a = 100$ ,  $X_1 = 100$  and  $X_2$  to  $X_4 = 0$   
therefore,

$$P_b = (100 + 100)/5 = 40$$

Similarly, in the third sampling cycle,  $P_b = 60$  is obtained; in the fourth sampling cycle,  $P_b = 80$ ; in the fifth sampling cycle,  $P_b = 100$ . In this manner,  $P_b$  is linearly increased. When the input  $P_a$  becomes zero, as shown in Fig. 7(a), the output  $P_b$  is also linearly decreased.

The linear acceleration/deceleration section 3 is operated as follows.

The high-order digital low-pass filter 4 will be described. This filter 4 can be prepared by a combination of the first- and/or second-order elements. The transfer function of the first-order filter is given by equations (1) and (3) in the following manner:

$$H(S) = BW_0 / (S + BW_0)$$

This transfer function is Z-transformed to obtain a pulse transfer function as follows:

$$H(Z) = G / (1 - K \cdot Z^{-1})$$

This pulse transfer function is achieved by the circuit shown in Fig. 8.

Referring to Fig. 8, reference numeral 12 denotes a multiplying means; and 13, an adding means. Reference symbol  $Z^{-1}$  denotes a delay unit for delaying an input by one sampling period  $T$ . Reference symbols  $K$  and  $G$  are values given as follows:

$$\begin{aligned} K &= e^{-BW_0 T} \\ G &= 1 - K \end{aligned}$$

When the operation of the circuit shown in Fig. 8 is performed for every sampling period  $T$ , a first-order digital filter can be obtained. In other words, the operations are performed as follows to obtain  $Y_0$ :

$$10 \quad Y_0 = G \cdot X + K \cdot Y_1$$

Similarly, a Z-transformed pulse transfer function of the second-order transfer function  $H$  given by equation (2) is derived as follows:

This transfer function is achieved by a circuit shown in Fig. 9. The following operations are performed for every sampling period  $T$  so as to obtain an output  $Y_0$ , thereby obtaining a second-order digital filter.

$y_1 = y_0$  ( $y_1$  is the immediately preceding sampled value of the sampled value  $y_0$ )

$$\text{for } K = 2 \cdot e^{-AW_0 T/2Q} \cdot \cos(AW_0 T \sqrt{4Q^2 - 1/2Q})$$

$$G = 1 - K - L$$

For example, in order to obtain a third-order

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filter, an output from the circuit shown in Fig. 8 is supplied to the circuit shown in Fig. 9. In other words, the first- and second-order filter operations are successively performed as follows:

$$\begin{aligned} Y_1 &= Y_0 \\ Y_0 &= G_1 \cdot X + K_1 \cdot Y_1 \\ Z_2 &= Z_1 \\ Z_1 &= Z_0 \\ Z_0 &= G_2 \cdot Y_0 + K_2 \cdot Z_1 + L_2 \cdot Z_2 \end{aligned}$$

The output  $Z_0$  is thus obtained from the third-order digital filter.

The standard values of the respective coefficients  $Q$ ,  $A$  and  $B$  in the Bessel filter are given below:

For the second-order filter:

$$Q = 0.5774 \text{ and } A = 1.732$$

For the third-order filter:

$$Q = 0.6911, A = 2.542 \text{ and } B = 2.322$$

For the fourth-order filter:

$$Q_1 = 0.5219, A_1 = 3.023, Q_2 = 0.8055 \text{ and } A_2 = 3.389$$

When the values of the coefficients  $Q$ ,  $A$  and  $B$  (especially the value of coefficient  $Q$ ) are changed, a filter which does not overshoot in response to the step input can be obtained.

Another embodiment will be described wherein the low-pass filter 4 is coupled to the output of the linear acceleration/deceleration section 3 shown in Fig. 4. The linear acceleration/deceleration control shown in Fig. 6 is performed, and a resultant output is processed by the three-order low-pass filter shown in Fig. 10 under the control of a microprocessor or the like. This operation will be described with reference to a flow chart shown in Fig. 11.

The coefficients  $Q$ ,  $A$  and  $B$  of the Bessel third-order filter, the cutoff frequency  $f_0$  of this filter, the sampling period  $T$  and the time interval for which acceleration/deceleration is started and

continues until a preset value is obtained are preset to obtain the respective coefficients  $K_1$ ,  $G_1$ ,  $K_2$ ,  $L_2$ ,  $G_2$  and  $n$  ( $= \tau/T$ ). The obtained values are entered in a microprocessor for controlling a robot or a machine tool (the respective coefficients  $K_1$ ,  $G_1$ ,  $K_2$ ,  $L_2$  and  $G_2$  may be calculated by the microprocessor). The processing shown in Fig. 11 is performed for every sampling period  $T$ .

When the position instruction  $P_a$  for each axis which is calculated by an interpolating means is supplied to the linear acceleration/deceleration section 3 for every sampling period  $T$ , the operation shown in Fig. 6 and given by equation (5) is performed. More specifically, the input value  $P_a$  and each of the delayed values  $X_1$  to  $X_{n-1}$  stored in the memory are added. The resultant sum is divided by  $n$ . The obtained value  $P_b$  is then stored in the memory (step 101). At the same time, the memory contents for the values  $X_1$  to  $X_{n-1}$  are shifted (steps 102-1 to 102-N-2) in such a manner that the value of  $X_{n-2}$  is stored in a memory area for  $X_{n-1}$  (step 102-1), the value of  $X_{n-3}$  is stored in a memory area for  $X_{n-2}$  (step 102-2), ... the value of  $X_1$  is stored in a memory area for  $X_2$  (step 102-N-2), and the input  $P_a$  is stored in a memory area for  $X_1$  (step 103). This processing is the linear acceleration/deceleration processing  $F_1$ .

The third-order low-pass filter processing  $F_2$  is then performed. Stored data from the memory area for  $Y_0$  is shifted to the memory area for  $Y_1$  (step 104). By using the value  $P_b$  obtained by the linear acceleration/deceleration processing  $F_1$  and the value  $Y_1$ , the following operation is performed:

$$Y_0 = G_1 P_b + K_1 Y_1$$

The resultant value of  $Y_0$  is stored in the memory (step 105). The values stored in the memory areas for  $Z_2$  and  $Z_1$  are updated to the values stored in the memory areas for  $Z_1$  and  $Z_0$  (steps 106 and 107). The following step

is executed, and the resultant value of  $Z_0$  is stored (step 108).

$$Z_0 = G_2 Y_0 + K_2 Z_1 + L_2 Z_2$$

The value stored in the memory area for  $Z_0$  is generated as  $P_c$  (step 109).

When the processing  $F_1$  and the processing  $F_2$  are executed for every timing period, the output  $P_b$  from the linear acceleration/deceleration section 3 in response to the input  $P_a$  is shown in Fig. 5(b), and the output  $P_c$  from the low-pass filter 4 is given as a smooth waveform signal, as shown in Fig. 5(c). The output  $P_c$  is supplied to the servo control section 6, high-speed acceleration/deceleration control can be performed without subjecting the servo control section 6, the servo motor M and the like to shock.

In the embodiment described with reference to the flow of Fig. 11, the processing  $F_2$  of the low-pass filter is performed after the linear acceleration/deceleration processing according to the acceleration/deceleration system shown in Fig. 4. However, according to an acceleration/deceleration system having the acceleration/deceleration section consisting of only a low-pass filter, only the processing  $F_2$  of Fig. 11 can be executed. In this case,  $P_b = P_a$  is established.

According to the present invention as described above, the high-frequency component is cut off by the higher-order low-pass filter, and a fast response time can be obtained. Therefore, the servo control system and its load system will not be subjected to shock, and precise control can be performed.

C L A I M S

1. An acceleration/deceleration control system of  
a servo motor, characterized in that a position  
instruction is filtered through a low-pass filter of  
5 second or higher order, thereby performing accelera-  
tion/deceleration control of the servo motor.

2. A system according to claim 1, characterized  
in that said low-pass filter comprises a Bessel filter.

3. An acceleration/deceleration control system of  
10 a servo motor, characterized in that a position  
instruction is subjected to linear acceleration/decel-  
eration control and thereafter is filtered through a  
low-pass filter of second or higher order.

4. A system according to claim 3, wherein said  
15 low-pass filter comprises a Bessel filter.

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FIG. 1

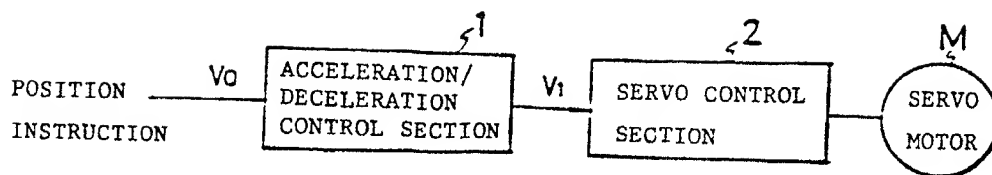


FIG. 2

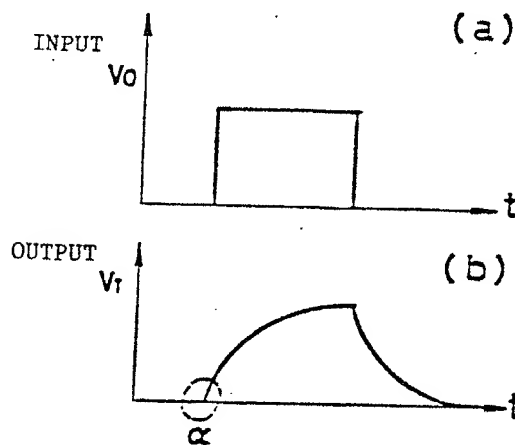


FIG. 3

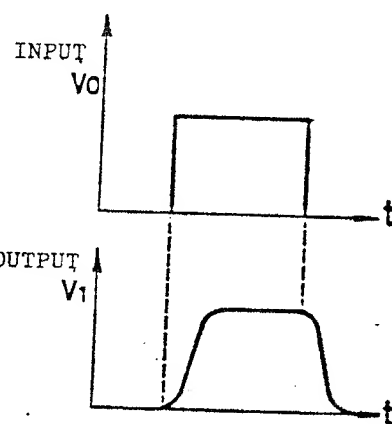


FIG. 4

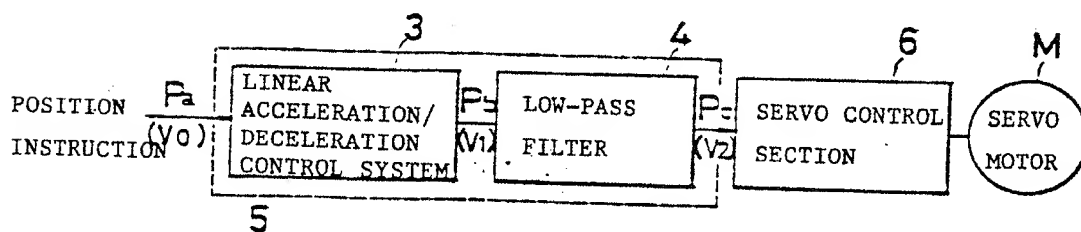


FIG. 5

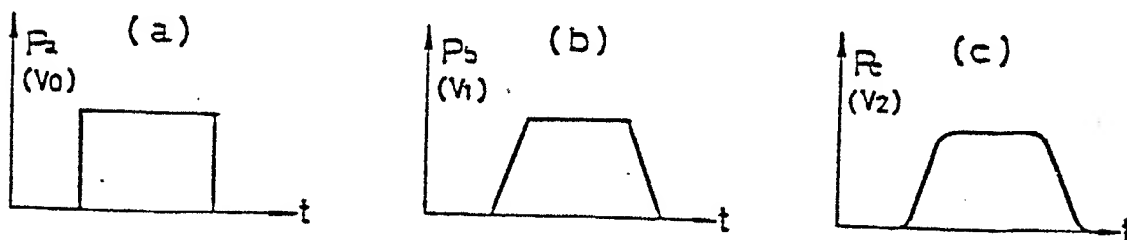


FIG. 6

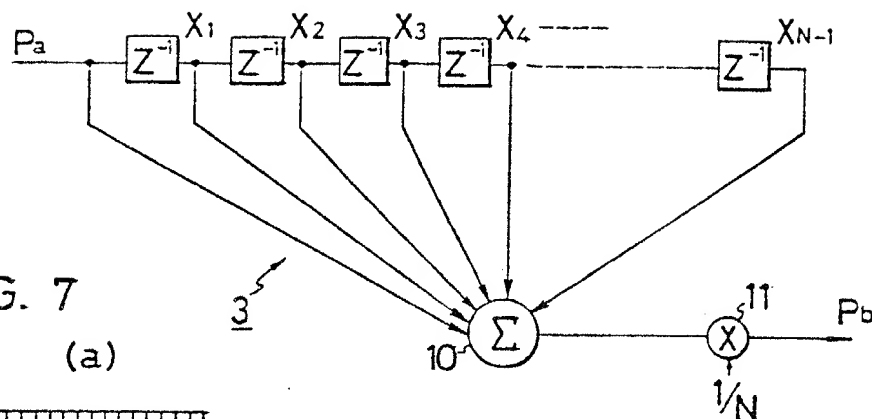


FIG. 7

(a)

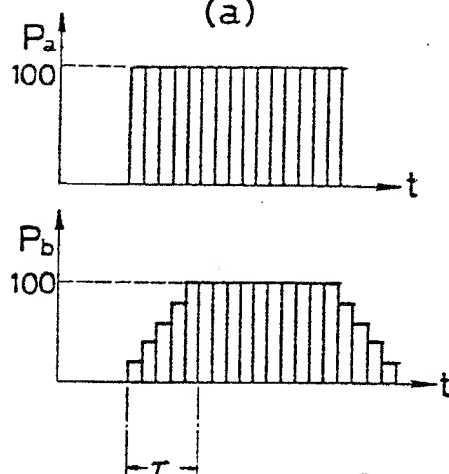


FIG. 8

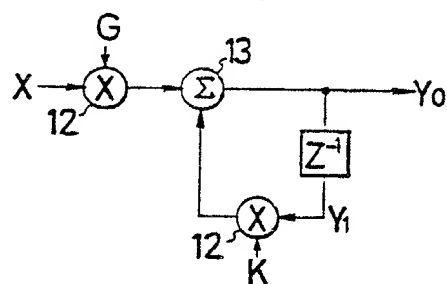


FIG. 9

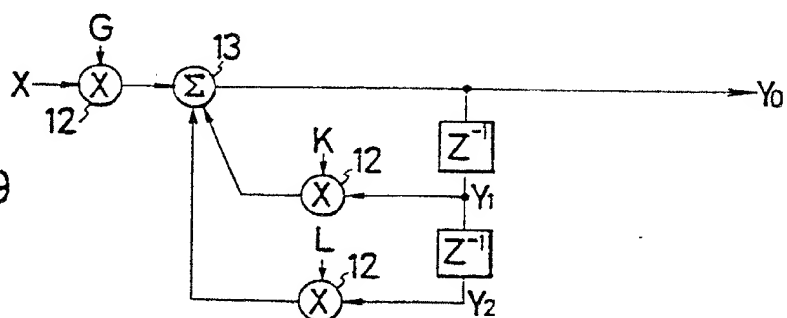


FIG. 10

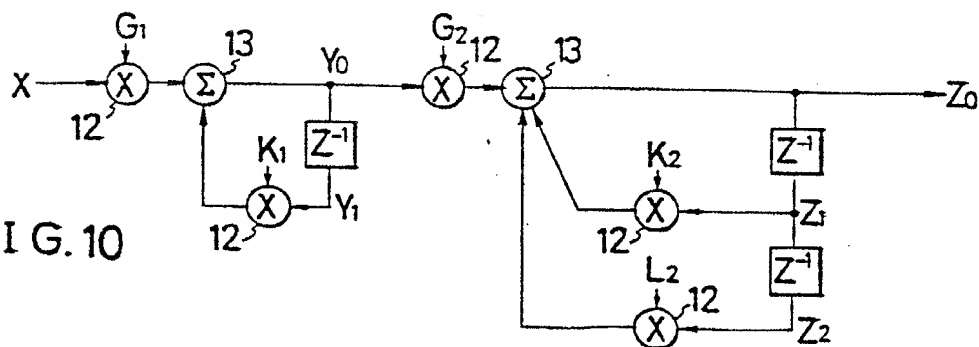
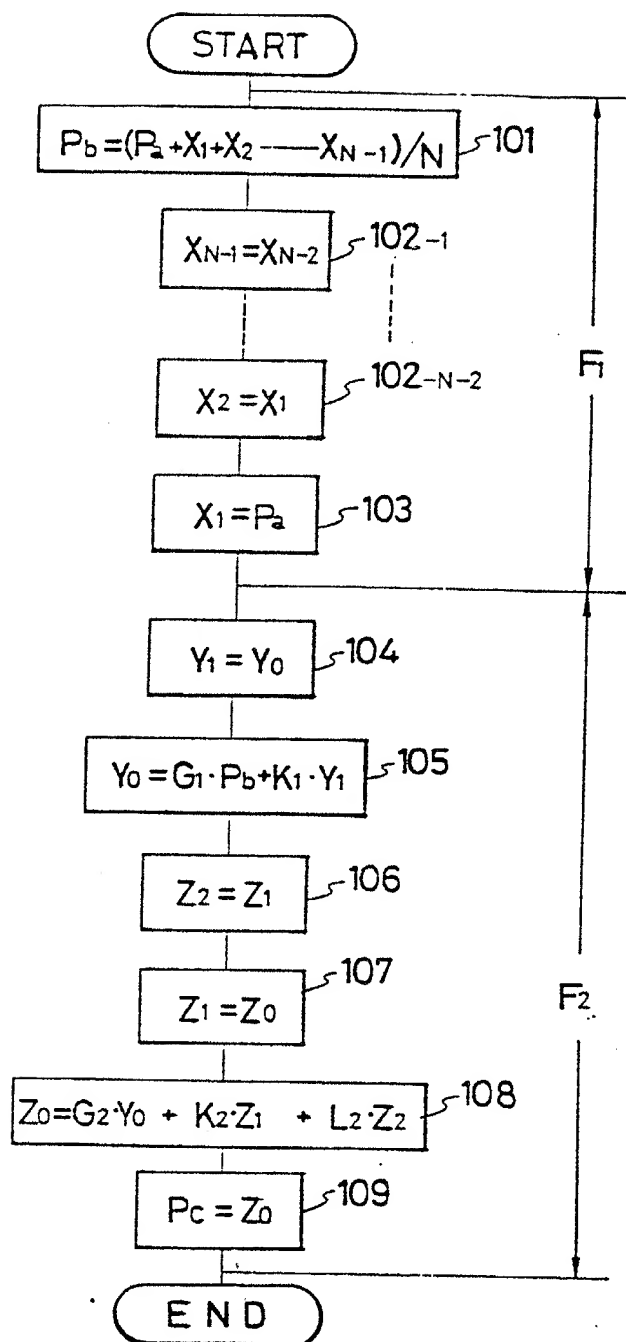




FIG. 11



## INTERNATIONAL SEARCH REPORT

0139010

International Application No.

PCT/JP84/00068

<b>I. CLASSIFICATION OF SUBJECT MATTER</b> (If several classification symbols apply, indicate all) <sup>1</sup>		
According to International Patent Classification (IPC) or to both National Classification and IPC Int. Cl. <sup>3</sup> G05B 11/36, G05D 3/00		
<b>II. FIELDS SEARCHED</b>		
Minimum Documentation Searched <sup>4</sup>		
Classification System	Classification Symbols	
IPC	G05B 11/00 - 11/42, 19/00 - 19/42 G05D 3/00 - 3/14 H02P 7/00	
Documentation Searched other than Minimum Documentation to the Extent that such Documents are included in the Fields Searched <sup>4</sup>		
Jitsuyo Shinan Koho		1960 - 1984
Kokai Jitsuyo Shinan Koho		1971 - 1984
<b>III. DOCUMENTS CONSIDERED TO BE RELEVANT</b> <sup>14</sup>		
Category <sup>15</sup>	Citation of Document, <sup>16</sup> with indication, where appropriate, of the relevant passages <sup>17</sup>	Relevant to Claim No. <sup>18</sup>
X	JP, A, 48-41214 (Mitsubishi Electric Corp.) 16 June 1973 (16. 06. 73)	1 - 4
X	JP, A, 48-59316 (Toshiba Corp.) 20 August 1973 (20. 08. 73)	1 - 4
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<b>IV. CERTIFICATION</b>		
Date of the Actual Completion of the International Search <sup>1</sup>		Date of Mailing of this International Search Report <sup>2</sup>
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International Searching Authority <sup>1</sup>		Signature of Authorized Officer <sup>20</sup>
Japanese Patent Office		

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